

## Physics 435 Final Information and Endgame

- 1) You must turn in Homework 11 by Wednesday, April 30 < 5pm to receive credit. This is the day of the last lecture.
  - a) I will post all homework solutions by Wednesday evening to help you prepare.
  - b) I will hold special office hours on Tuesday, April 29 from 2:30 – 4:30 pm to help with this homework.
  
- 2) Be sure to check that all of your grades are correctly recorded prior to the last day of class. In particular, make sure that your HW 3 are now correctly recorded since grades were lost due to a disk crash early in the semester.
  
- 3) The final exam will be held in 136 Loomis on Saturday, May 3<sup>rd</sup> from 8 am – 11 am
  - a) The final exam will be comprehensive covering all topics in the course up to and including the Electrodynamics chapter.
  - b) I will hold special office hours on Wednesday April 30 from 2:30 – 4:30 pm and on Reading Day, Thursday May 1 from 2:30 - 4:30 pm to answer questions about the final.
  - c) I will work the (attached) final review problem on the Wednesday, April 30 lecture.
  - d) If you arrive on time for the exam on Saturday you will have 3 hours to work the exam.
    - i) There will be five problems on the final
    - ii) Unlike the midterms you will need to turn in both your answers and the exam questions to receive credit.
    - iii) The final exam is open book and open notes like the midterm.

Here is a problem (with some hopefully correct answers) that we will discuss on the last lecture of class on April 30 on time varying fields.

Consider a long, conducting inner cylinder of radius  $a$  and length  $L$  which carries a surface current of  $\vec{K}_a = K \hat{z}$ . A coaxial log cylinder of radius  $b$  and length  $L$  carries a surface current of  $\vec{K}_b$  with  $b > a$ . Answer all parts in terms of  $K, a, b, L, \omega$ , cylindrical coordinates and physical constants as needed.

(a) Find  $\vec{K}_b$  that insures that  $\vec{B}(s > b) = 0$ . Assume this  $\vec{K}_b$  is present in all parts of this problem

(b) Calculate  $\vec{B}(a < s < b)$  using Ampere's Law.

(c) Compute  $\vec{A}$  in all regions using  $\int_s \vec{A} \cdot d\vec{\ell} = \int_s \vec{B} \cdot d\vec{a}$

$$\text{answer: } \vec{A}(a < s < b) = -\hat{z} \mu_0 a K \ln \frac{s}{a}$$

(d) Check continuity of  $\vec{A}$  and discontinuity of  $\frac{\partial \vec{A}}{\partial s}$  at the boundaries  $s = a$  and  $s = b$ .

We now oscillate the inner conductor current according to  $\vec{K} = K \sin \omega t \hat{z}$ .

(e) Compute  $\vec{E}$  to first order in  $\omega$  using Faraday's Law. Hint- the electric field is along the  $z$ -direction and the loop integral was mostly done in part (c).

$$\text{answer: } \vec{E} = \hat{z} \mu_0 a K \ln \frac{s}{a} \omega \cos \omega t$$

(f) Check the  $\vec{E}$  expression you computed in part (e) using  $\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ .

(g) Calculate  $\vec{B}$  to second order in  $\omega^2$  by using the displacement current from the  $\vec{E}$  expression you computed in part (e). This integral may be helpful

$$\int v \ln v \, dv = \frac{v^2}{4} (2 \ln v - 1).$$

$$\text{answer: } \vec{B} = \hat{\phi} \frac{\mu_0 a K}{s} \sin \omega t \left[ 1 - \frac{\omega^2}{4c^2} \left( a^2 - s^2 + 2s^2 \ln \frac{s}{a} \right) + \mathcal{O}(\omega^4) \right]$$

(h) Check your result by showing  $\vec{\nabla} \times \vec{B} = \frac{1}{c^2} \frac{\partial \vec{E}}{\partial t}$  in the region  $a < s < b$ .